

Northwestern University  
Department of Computer Science  
Department of Electrical and Computer Engineering

Teachers: Robert Dick                      Peter Dinda  
Office: L477 Tech                              338, 1890 Maple Ave.  
Email: dickrp@ece.northwestern.edu      pdinda@cs.northwestern.edu  
Phone: 467-2298                              467-7859  
Webpage: <http://ziyang.ece.northwestern.edu/EXTERNAL/realtime>

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## Goals for lecture

- Handle a few administrative details
- Form lab groups
- Broad overview of real-time systems
- Definitions that will come in handy later
- Example of real-time sensor network

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## Backgrounds

- Lab teams had best be balanced (low-level vs. high-level experience)
- Name
- Which are you better at?
  - Low-level ANSI-C/assembly experience
  - High-level object-oriented programming experience
- What's your major?

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## Core course goal

By the end of this course, we want you to learn how to build real-time systems and build a useful real-time sensor network.

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## Administrative tasks

- Backgrounds
- Question rule
- Office hours

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## Question rule

- If something in lecture doesn't make sense, please ask
- You're paying a huge amount of money for this
- Letting something important from lecture slip by for want of a question is like burning handfuls of money

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## Office hours

- When shall I schedule my office hours?

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## Today's topics

- Taxonomy of real-time systems
- Optimization and costs
- Definitions
- Optimization formulation
- Overview of primary areas of study within real-time systems

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## Taxonomy: Static

- Task arrival times can be predicted.
- Static (compile-time) analysis possible.
- Allows good resource usage (low processor idle time proportions).
- Sometimes designers shoehorn dynamic problems into static formulations allowing a good solution to the wrong problem.

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## Taxonomy: Soft real-time

- More slack in implementation
- Timing may be suboptimal without being incorrect
- Problem formulation can be much more complicated than hard real-time
- Two common (and one uncommon) methods of dealing with non-trivial soft real-time system requirements
  - Set somewhat loose hard timing constraints
  - Informal design and testing
  - Formulate as optimization problem

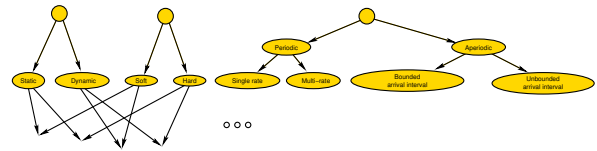
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## Taxonomy: Periodic

- Each task (or group of tasks) executes repeatedly with a particular period.
- Allows some nice static analysis techniques to be used.
- Matches characteristics of many real problems...
- ... and has little or no relationship with many others that designers try to pretend are periodic.

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## Taxonomy of real-time systems



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## Taxonomy: Dynamic

- Task arrival times unpredictable.
- Static (compile-time) analysis possible only for simple cases.
- Even then, the portion of required processor utilization efficiency goes to 0.693.
- In many real systems, this is very difficult to apply in reality (more on this later).
- Use the right tools but don't over-simplify, e.g.,
  - We assume, without loss of generality, that all tasks are independent.*
- If you do this people will make jokes about you.

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## Taxonomy: Hard real-time

- Difficult problem. Some timing constraints inflexible.
- Simplifies problem formulation.

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## Taxonomy: Periodic → Single-rate

- One period in the system.
- Simple.
- Inflexible.
- This is how a *lot* of wireless sensor networks are implemented.

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## Taxonomy: Periodic → Multirate

- Multiple periods.
- Can use notion of circular time to simplify static (compile-time) schedule analysis E. L. Lawler and D. E. Wood, "Branch-and-bound methods: A survey," *Operations Research*, pp. 699–719, July 1966.
- Co-prime periods leads to analysis problems.

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## Taxonomy: Aperiodic

- Also called sporadic, asynchronous, or reactive
- Implies dynamic
- Bounded arrival time interval permits resource reservation
- Unbounded arrival time interval impossible to deal with for any resource-constrained system

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## Definitions: Task

- Some operation that needs to be carried out
- Atomic completion: A task is all done or it isn't
- Non-atomic execution: A task may be interrupted and resumed

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## Task/processor relationship

	WC exec time (s)	
Tooth	7.7E-6	...
Road	330E-9	...
FIR	4.1E-6	...
Matrix	310E-3	...

IDT79RC32364 100 MHz  
 Imsys Cijp 40 MHz  
 IBM PowerPC 405GP 266 MHz

Relationship between tasks, processors, and costs  
 E.g., power consumption or worst-case execution time

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## Taxonomy: Periodic → Other

- It is possible to have tasks with deadlines less than, equal to, or greater than their periods.
- Results in multi-phase, circular-time schedules with multiple concurrent task instances.
  - If you ever need to deal with one of these, see me (take my code). This class of scheduler is nasty to code.

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## Definitions

- Task
- Processor
- Graph representations
- Deadline violation
- Cost functions

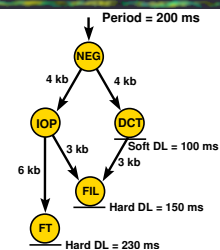
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## Definitions: Processor

- Processors execute tasks
- Distributed systems
  - Contain multiple processors
  - Inter-processor communication has impact on system performance
  - Communication is challenging to analyze
- One processor type: Homogeneous system
- Multiple processor types: Heterogeneous system

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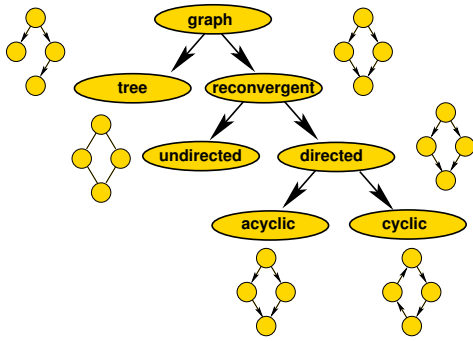
## Graph definitions



- Set of vertices ( $V$ )– usually operations
- Set of edges ( $E$ )– directed or undirected relationships on vertex pairs

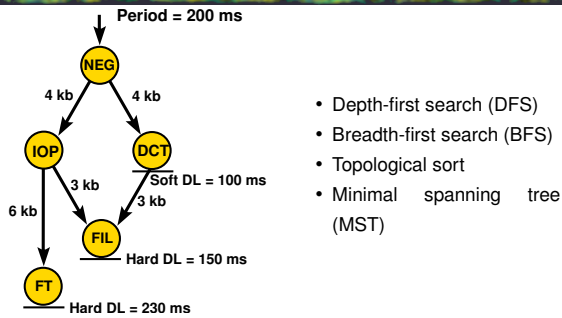
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## Example graph classifications



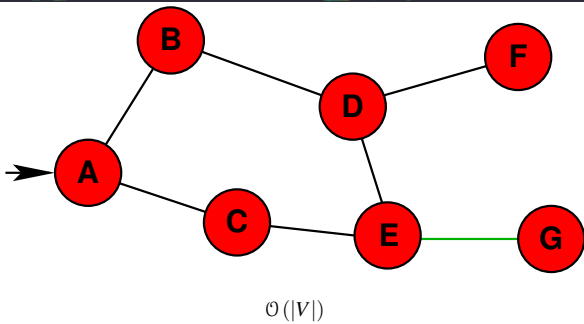
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## A few basic graph algorithms



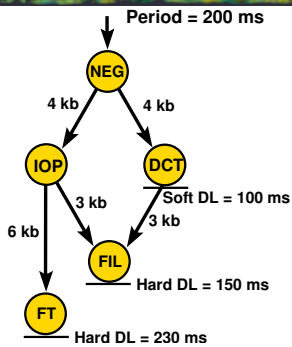
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## Breadth-first search (BFS) – Pre-order for trees



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## Definition: Deadline violation



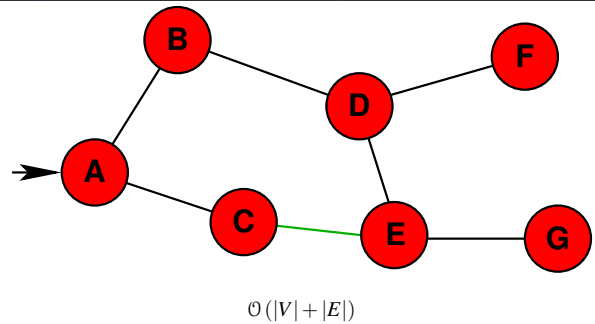
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## Some graph uses

- Problem representations
- Timing constraint specification
- Resource binding
- And many more...

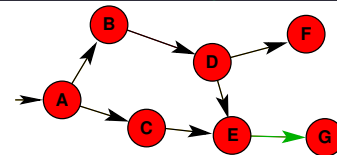
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## Depth-first search (DFS) – Pre-order for trees



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## Topological sort



Static timing analysis of data-dependent real-time systems

- Earliest finish time (EFT)
- Latest finish time (LFT)
- Earliest start time (EST)
- Latest start time (LST)

$O(|V| + |E|)$

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## Cost functions

- Mapping of real-time system design problem solution instance to cost value
- I.e., allows price, or hard deadline violation, of a particular multi-processor implementation to be determined

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## Back to real-time problem taxonomy:

### Jagged edges

- Some things dramatically complicate real-time scheduling
- These are horrific, especially when combined
  - Data dependencies
  - Unpredictability
  - Distributed systems
- These are irksome
  - Heterogeneous processors
  - Preemption

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### Allocation, assignment and scheduling

How does one best

- Analyze problem instance specifications
  - E.g., worst-case task execution time
- Select (and build) hardware components
- Select and produce software
- Decide which processor will be used for each task
- Determine the time(s) at which all tasks will execute

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### Operating systems and scheduling

How does one best design operating systems to

- Support sufficient detail in workload specification to allow good control, e.g., over scheduling, without increasing design error rate
- Design operating system schedulers to support real-time constraints?
- Support predictable costs for task and OS service execution

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### The value of formality: Optimization and costs

- The design of a real-time system is fundamentally a cost optimization problem
- Minimize costs under constraints while meeting functionality requirements
  - Slight abuse of notation here, functionality requirements are actually just constraints
- Why view problem in this manner?
- Without having a concrete definition of the problem
  - How is one to know if an answer is correct?
  - More subtly, how is one to know if an answer is optimal?

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## Central areas of real-time study

- Allocation, assignment and **scheduling**
- Operating systems and **scheduling**
- Distributed systems and **scheduling**
- **Scheduling is at the core of real-time systems study**

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### Allocation, assignment and scheduling

- In order to efficiently and (when possible) optimally minimize
  - Price, power consumption, soft deadline violations
- Under hard timing constraints
- Providing guarantees whenever possible
- For all the different classes of real-time problem classes

This is what I did for a Ph.D.

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### Distributed systems and scheduling

How does one best dynamically control

- The assignment of tasks to processing nodes...
- ... and their schedules

for systems in which computation nodes may be separated by vast distances such that

- Task deadline violations are bounded (when possible)...
- ... and minimized when no bounds are possible

This is part of what Professor Dinda did for a Ph.D.

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### Optimization

Thinking of a design problem in terms of optimization gives design team members objective criterion by which to evaluate the impact of a design change on quality.

- Still need to do a lot of hacking
- Know whether its taking you in a good direction

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## Summary

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- Real-time systems taxonomy and overview
- Definitions
- Importance of problem formulation

## Reading assignment (for next class)

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- J. W. S. Liu, *Real-Time Systems*. Prentice-Hall, Englewood Cliffs, NJ, 2000
- Chapter 2
- Start on Chapter 3